



Integrating Models and Data for Robust Manipulation with and around people



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Manipulation

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Physics-based Manipulation

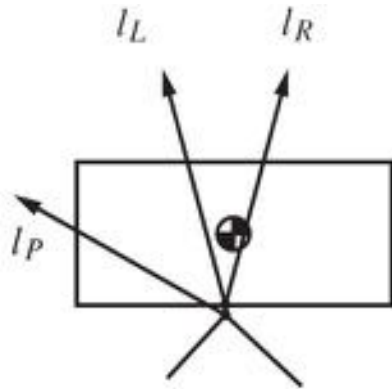
DARPA ARM-S

CMU 2010-13

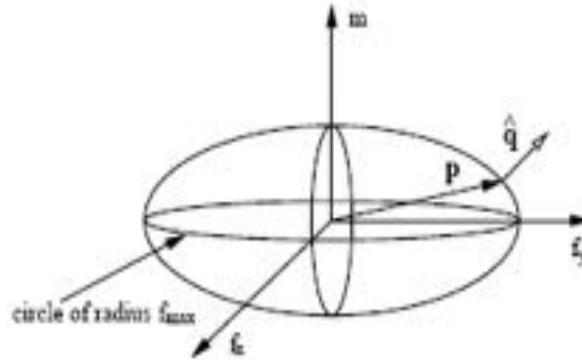


Harness the Mechanics of Manipulation
to Funnel Uncertainty

Quasi-Static Pushing



The Voting Theorem
[Mason'81]

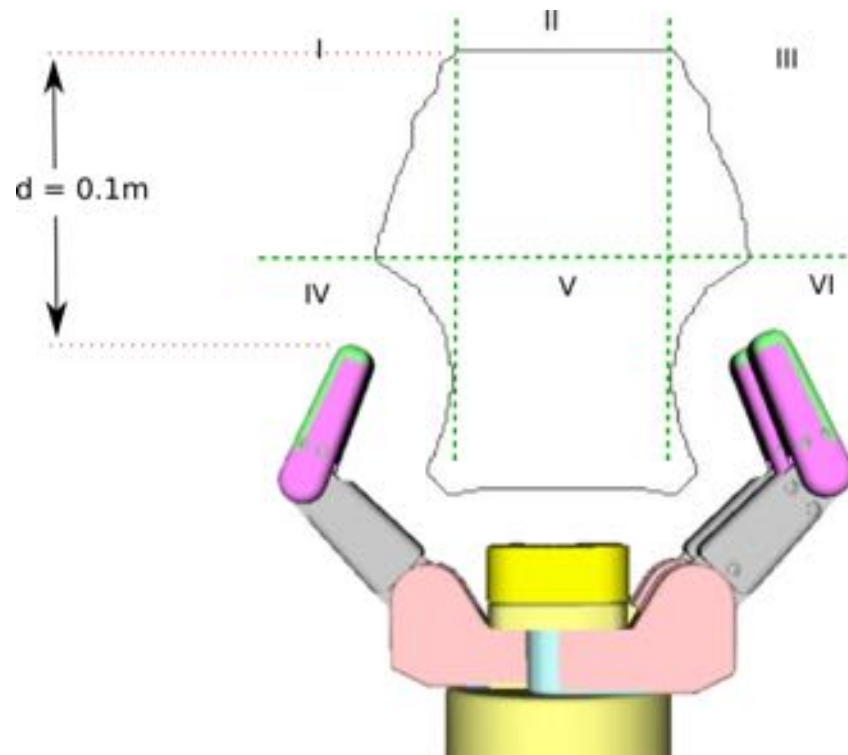
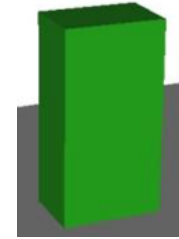


The Limit Surface
[Goyal et al.'91, Howe and Cutkosky'96]

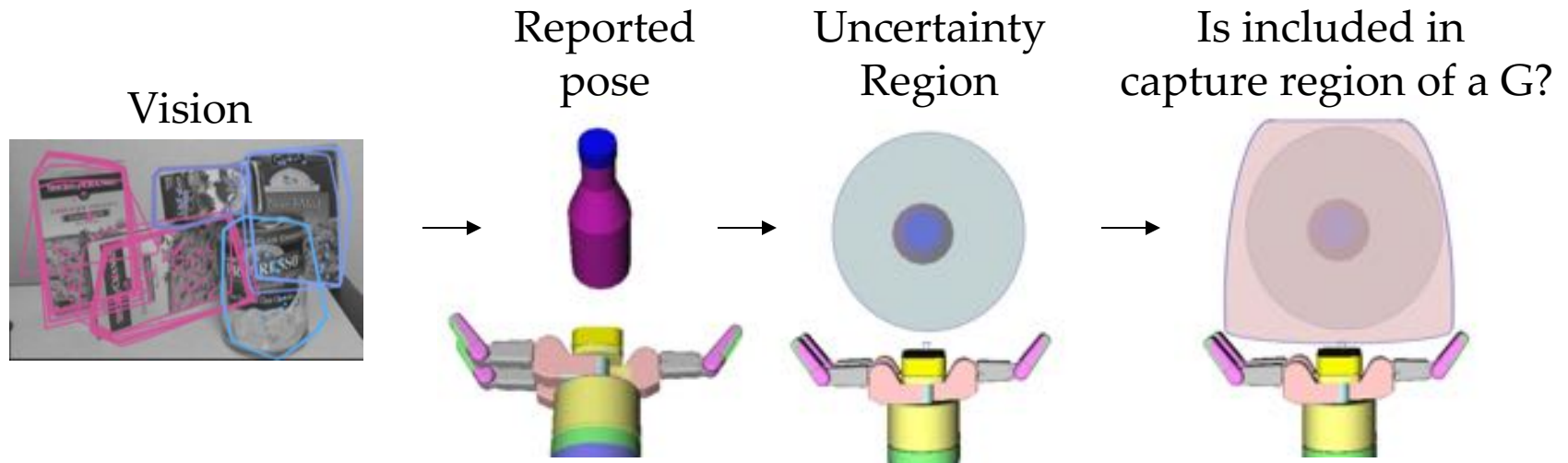
How much should the robot know?

- Object mass? No.
- Object-surface friction? No.
- Object pressure distribution? Pick conservatively.
- Finger-object friction? Pick conservatively.

Analytical Capture Regions



Addressing Object Pose Uncertainty

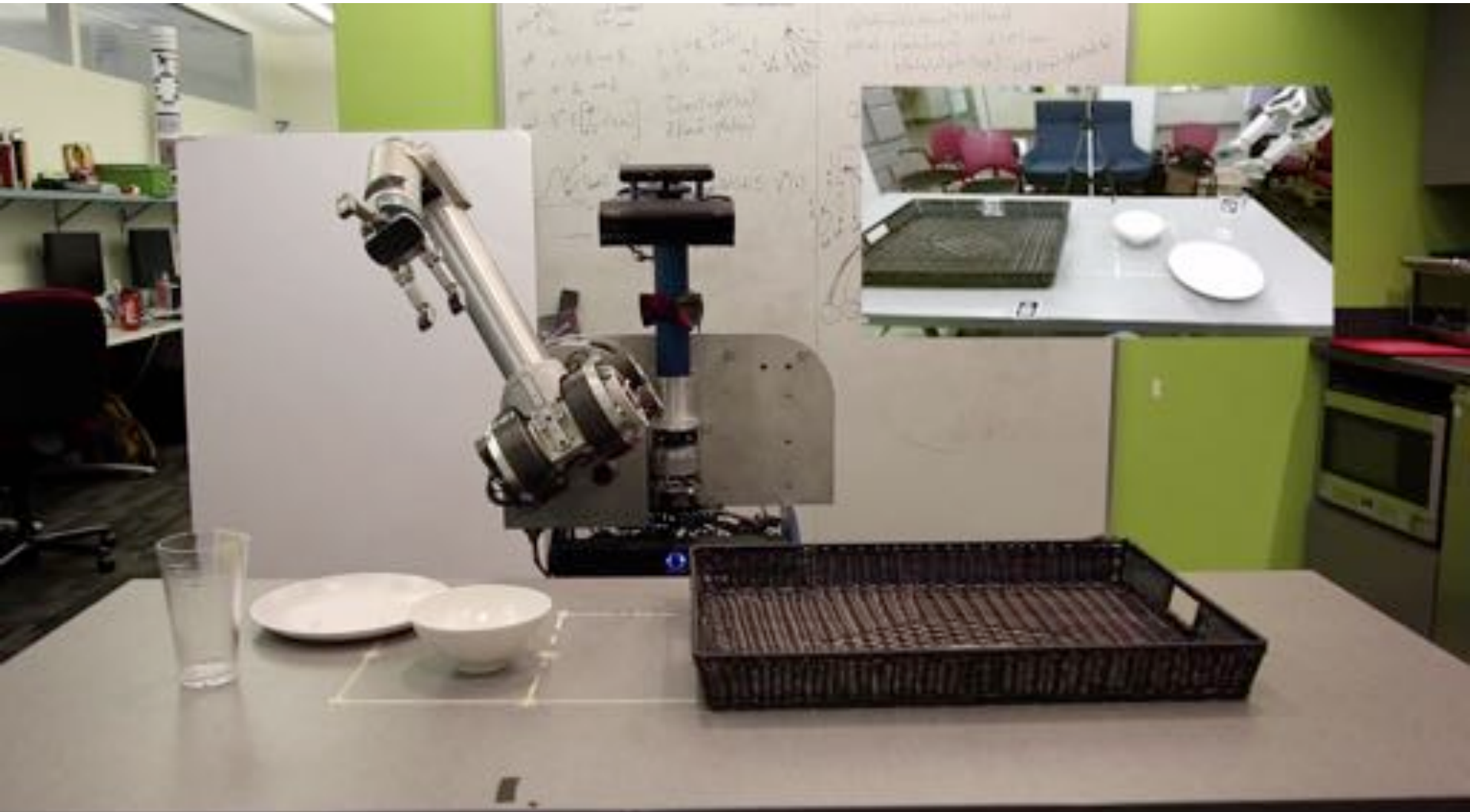


Physics-based Manipulation

Exploiting physics to manipulate objects



Autonomous control of complex dynamical systems



Global models are often
only partially correct

Optimal Control

Model-based RL



	Global, analytical models		
Model	Inaccurate		
Policy	No uncertainty		
Data	No data collection		
Training	Fast convergence		

Optimal Control

Model-based RL



	Global, analytical models		Locally learned models
Model	Inaccurate		Locally more accurate, captures uncertainty
Policy	No uncertainty		Uncertainty-aware
Data	No data collection		Requires data collection
Training	Fast convergence		Slow convergence

Optimal Control

Model-based RL



	Global, analytical models	Hybrid model	Locally learned models
Model	Inaccurate	Globally available, Locally accurate, captures uncertainty	Locally more accurate, captures uncertainty
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Training	Fast convergence	Moderate	Slow convergence

Learn the **residual** between simulation and reality

Gaussian Process Regression



Gilwoo Lee

Optimal Control

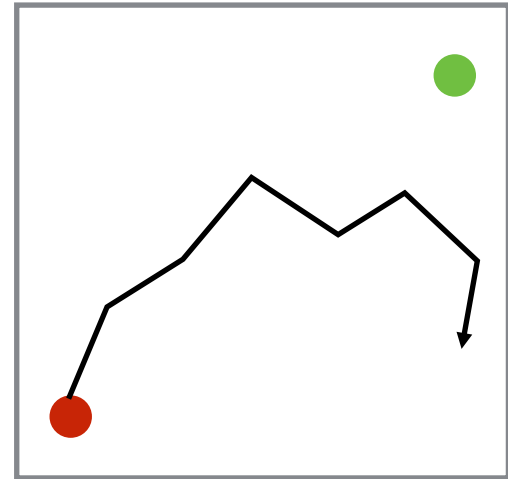
Model-based RL



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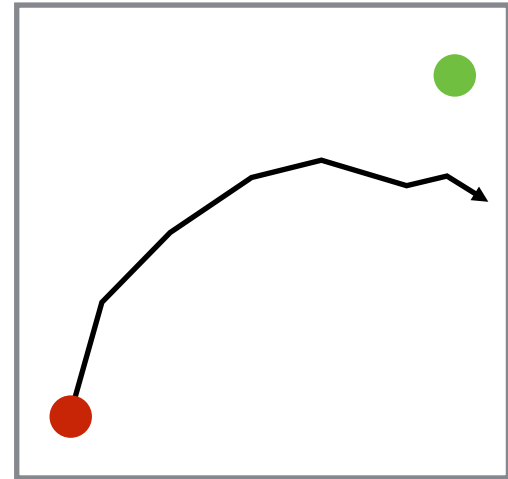
Policy Search: Iterative Linear Quadratic Regulator

Linear dynamics,
Quadratic cost,
Iterative local improvements



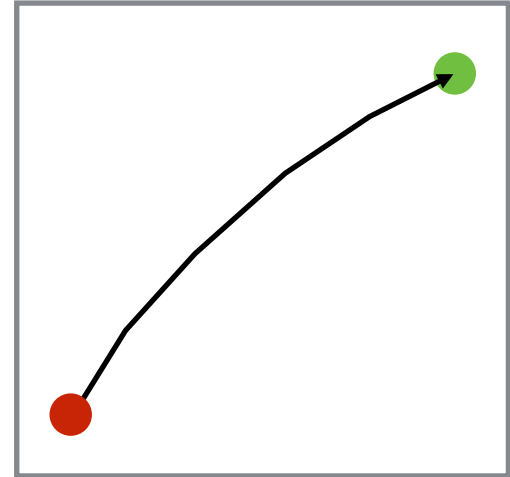
Policy Search: Iterative Linear Quadratic Regulator

Linear dynamics,
Quadratic cost,
Iterative local improvements



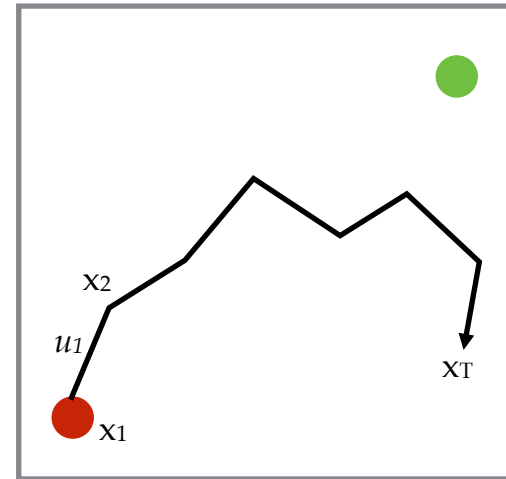
Policy Search: Iterative Linear Quadratic Regulator

Linear dynamics,
Quadratic cost,
Iterative local improvements



Policy Search: Iterative Linear Quadratic Gaussian Control

Linear **stochastic** dynamics,
Quadratic cost,
Iterative local improvements



Incorporate **model uncertainty** into the Iterative Linear Quadratic Regulator

Robust Iterative Linear Quadratic Regulator

Policy Search: Iterative Linear Quadratic Gaussian Control

$$\mathbf{x}_{t+1} = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) + \boldsymbol{\zeta}(\mathbf{x}_t, \mathbf{u}_t), \quad \boldsymbol{\zeta} \sim \mathcal{N}(0, \Gamma)$$

Bellman update:

$$V(\mathbf{x}_t) = \min_{\mathbf{u}_t} \boxed{l(\mathbf{x}_t, \mathbf{u}_t) + \mathbb{E}[V'(\mathbf{f}(\mathbf{x}_t, \mathbf{u}_t))]} \quad \mathcal{Q}$$

$$Q(\delta \mathbf{x}, \delta \mathbf{u}) = Q_x \delta \mathbf{x} + Q_u \delta \mathbf{u} + 1/2(\delta \mathbf{x}^T Q_{xx} \delta \mathbf{x} + \delta \mathbf{u}^T Q_{uu} \delta \mathbf{u} + 2 \delta \mathbf{x}^T Q_{xu} \delta \mathbf{u})$$

$$Q_x = l_x + \mathbb{E}[\mathbf{f}_x^T V'_x] = l_x + \mathbb{E}[(\mathbf{f} + \boldsymbol{\zeta})_x^T V'_x] = l_x + \mathbf{f}_x^T V'_x$$

$$Q_u = l_u + \mathbb{E}[\mathbf{f}_u^T V'_x]$$

$$Q_{xx} = l_{xx} + \mathbb{E}[\mathbf{f}_x^T V'_{xx} \mathbf{f}_x] = l_{xx} + \mathbb{E}[(\mathbf{f} + \boldsymbol{\zeta})_x^T V'_{xx} (\mathbf{f} + \boldsymbol{\zeta})_x] = l_{xx} + \mathbf{f}_x^T V'_{xx} \mathbf{f}_x + \mathbb{E}[\boldsymbol{\zeta}_x^T V'_{xx} \boldsymbol{\zeta}_x]$$

$$Q_{uu} = l_{uu} + \mathbb{E}[\mathbf{f}_u^T V'_{xx} \mathbf{f}_u]$$

$$Q_{ux} = l_{ux} + \mathbb{E}[\mathbf{f}_u^T V'_{xx} \mathbf{f}_x]$$

Policy Search: Robust ILQG

$$\begin{aligned} \mathbf{x}_{t+1} &= \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) + \zeta(\mathbf{x}_t, \mathbf{u}_t) \\ &= \mathbf{f}_{\text{global}}(\mathbf{x}_t, \mathbf{u}_t) + \boldsymbol{\mu}(\mathbf{x}_t, \mathbf{u}_t) + \boldsymbol{\xi}(\mathbf{x}_t, \mathbf{u}_t) + \zeta(\mathbf{x}_t, \mathbf{u}_t) \end{aligned} \quad \zeta \sim \mathbf{N}(0, \Gamma), \quad \boldsymbol{\xi} \sim \mathbf{N}(0, \Sigma)$$

Policy Search: Robust ILQG

$$\begin{aligned} \mathbf{x}_{t+1} &= \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) + \zeta(\mathbf{x}_t, \mathbf{u}_t) \\ &= \mathbf{f}_{\text{global}}(\mathbf{x}_t, \mathbf{u}_t) + \boldsymbol{\mu}(\mathbf{x}_t, \mathbf{u}_t) + \boldsymbol{\xi}(\mathbf{x}_t, \mathbf{u}_t) + \zeta(\mathbf{x}_t, \mathbf{u}_t) \end{aligned} \quad \zeta \sim \mathcal{N}(0, \Gamma), \quad \boldsymbol{\xi} \sim \mathcal{N}(0, \Sigma)$$

Bellman update:

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$$Q(\delta \mathbf{x}, \delta \mathbf{u}) = Q_x \delta \mathbf{x} + Q_u \delta \mathbf{u} + 1/2(\delta \mathbf{x}^T Q_{xx} \delta \mathbf{x} + \delta \mathbf{u}^T Q_{uu} \delta \mathbf{u} + 2 \delta \mathbf{x}^T Q_{xu} \delta \mathbf{u})$$

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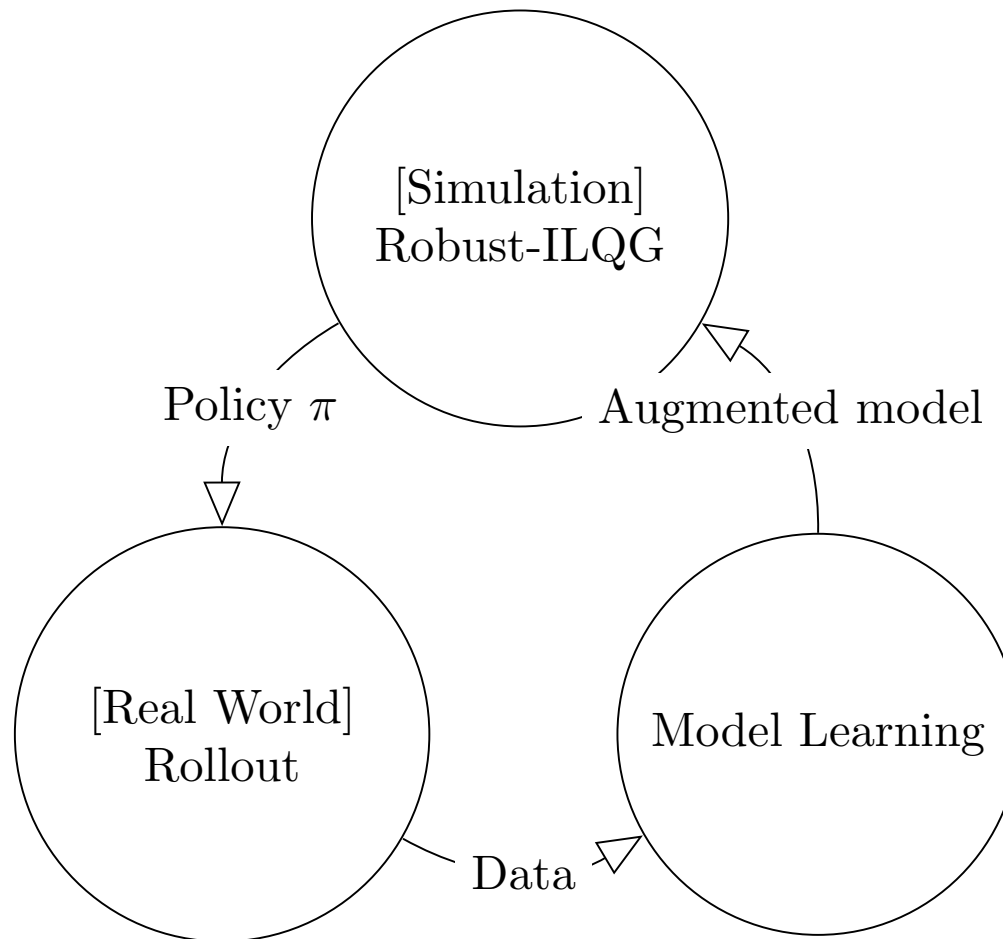
$$Q_{xx} = l_{xx} + \mathbb{E}[\mathbf{f}_x^T V'_{xx} \mathbf{f}_x] = l_{xx} + \mathbb{E}[(\mathbf{f}_{\text{global}} + \boldsymbol{\mu} + \boldsymbol{\xi} + \zeta)_x^T V'_{xx} (\mathbf{f}_{\text{global}} + \boldsymbol{\mu} + \boldsymbol{\xi} + \zeta)_x]$$

$$Q_{uu} = l_{uu} + \mathbb{E}[\mathbf{f}_u^T V'_{xx} \mathbf{f}_u]$$

$$Q_{ux} = l_{ux} + \mathbb{E}[\mathbf{f}_u^T V'_{xx} \mathbf{f}_x]$$

GP-ILQG

GP-ILQG: Data-driven Robust Optimal Control for Uncertain Nonlinear Dynamical Systems. Lee, Srinivasa, and Mason, 2017



Comparison

Optimal Control

Model-based RL



	Global, analytical models	Hybrid model	Locally learned models
Algorithm	ILQG	GP-ILQG	Probabilistic-DDP
	Assumes perfect model		Needs data
Initialization	Initialized with random policy	Initialized with ILQG policy & random trajectories	Random policy & Demonstrated trajectories

Todorov, Emanuel, and Weiwei Li. "A generalized iterative LQG method for locally-optimal feedback control of constrained nonlinear stochastic systems."

American Control Conference, 2005. Proceedings of the 2005. IEEE, 2005.

Pan, Yunpeng, and Evangelos Theodorou. "Probabilistic differential dynamic programming." *Advances in Neural Information Processing Systems*. 2014.

Optimal Control

Model-based RL



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Limitations

- Scaling of GPs

Use any learner that reports uncertainty

- Robustness to model error discourages exploration

Encourage exploration, e.g. posterior sampling

Takeaways

- Models are nice, but not perfect
Bootstrap models with data
- Strive for minimalism
Task-driven model learning



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